

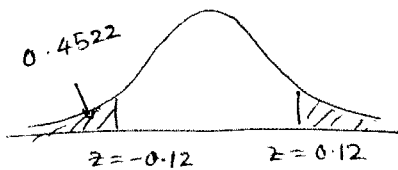
1) The null hypothesis always contains an equality and takes the value at which the claim is marginally false.

Therefore (B)

2) The smaller the p-value, the stronger the evidence against  $H_0$ .  
So if the p-value is to be consistent with  $H_0$ , p-value has to be large

Therefore (D)

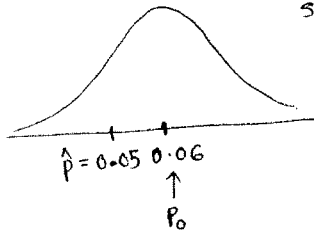
3) Since  $H_a: p \neq p_0$ , this is a two tail probability.



$$\begin{aligned} \text{therefore P-value} &= 2(0.4522) \\ &= 0.9044 \\ &= 0.90. \end{aligned}$$

4)  $H_0: p = 0.06$        $n = 100$

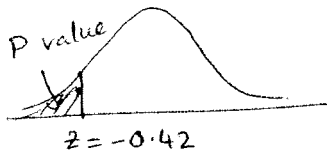
$H_a: p < 0.05$



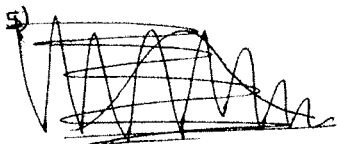
$$se = \sqrt{\frac{p_0(1-p_0)}{n}} = \sqrt{\frac{0.06(1-0.06)}{100}} = 0.0237.$$

$$z = \frac{\hat{p} - p_0}{se} = \frac{0.05 - 0.06}{0.0237} = -0.42$$

implies this is a left tail probability.

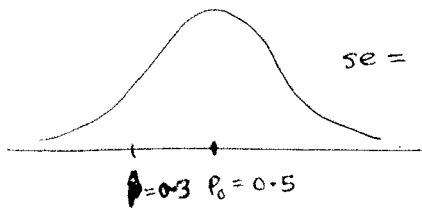


$$\begin{aligned} \text{P value} &= 0.3372 \\ &= 0.34. \end{aligned}$$



5)  $H_0: p = 0.5$        $n = 1933$

$\hat{p} = 0.3$



$$se = \sqrt{\frac{p_0(1-p_0)}{n}} = \sqrt{\frac{0.5(0.5)}{1933}} = 0.0114$$

$$z = \frac{\hat{p} - p_0}{se} = \frac{0.3 - 0.5}{0.0114} = -17.54$$

6)  ~~$P < \alpha$~~   
 $0.0485 < 0.05$

Therefore reject  $H_0$ . (Accept  $H_a$ )

(E)

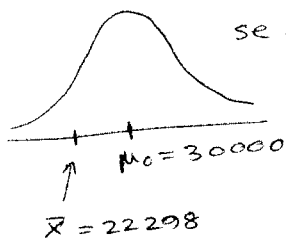
7)  $H_0: p = 0.4$        $P\text{-value} = 0.005 \leftarrow \text{very small.}$   
 $H_a: p > 0.4$

P-value is the probability that we can observe the observed value or values more extreme if  $H_0$  is true.

Therefore, if  $H_0$  is true, that is if the chlorine level has not changed, the probability of observing the sample chlorine level observed or more, higher values is 0.005. Therefore since P value is very less, reject  $H_0$ .  
 Therefore we conclude that the chlorine level has increased.

(C)

8)  $H_0: \mu = 30000$        $n = 17$        $\bar{x} = 22298$        $s = 14200$



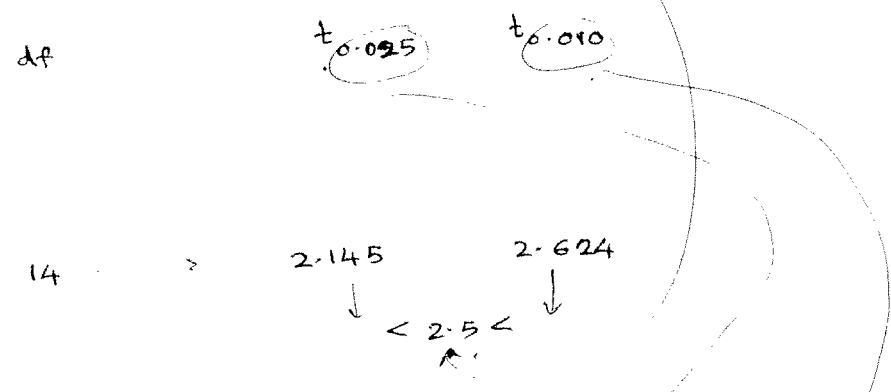
$$se = \frac{s}{\sqrt{n}} = \frac{14200}{\sqrt{17}} = 3444$$

$$t = \frac{\bar{x} - \mu_0}{se} = \frac{22298 - 30000}{3444} = -2.24$$

9)  $H_a: \mu \neq 12$ . therefore, this is a two tail probability.

Take  $|t| = |1 - 2.5| = 2.5$ ,

$df = 15 - 1 = 14$ .



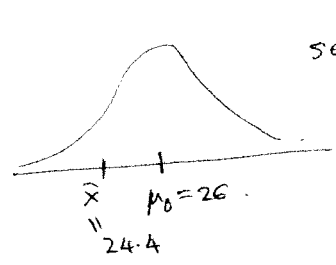
Since two tail P-value falls between  
 $2(0.010) < P < 2(0.025)$   
 $0.02 < P < 0.05$

(P-value cannot be 0.05 since for that t has to be 2.624)

therefore P-value = 0.025

10)  $H_0: \mu = 26$      $H_a: \mu < 26$      $n = 25$      $\bar{x} = 24.4$      $s = 9.2$

(since we are dealing with a mean and the sample size is small, we have to use t-score.)



$se = \frac{s}{\sqrt{n}} = \frac{9.2}{\sqrt{25}} = 1.84$

$t = \frac{\bar{x} - \mu_0}{se} = \frac{24.4 - 26}{1.84} = -0.87$

There is only one answer with  $t = -0.87$ . therefore (C).

(If there were two answers with  $t = -0.87$ , then we have to find the P-value to decide whether to reject or not reject  $H_0$ )

11)  $H_0: \mu = 46$

$H_a: \mu \neq 46$

Therefore two tail.

12)  $H_0: \mu = 500$

$H_a: \mu > 500$

right tail.

13) Type I error is when we reject a true  $H_0$ .

Therefore if we conclude  $\mu > 9.8$  (accepting  $H_a$  means rejecting  $H_0$ ), while in fact  $\mu = 9.8$ , it is a type I error.

(B)

14) Failing to reject a false null hypothesis is Type II error.

The test failed to reject  $H_0$ . However,  $\mu \neq 9.4$ . (That is  $H_0$  is false).

Therefore Type II error.