

1) point estimate for population proportion = sample proportion

$$= \frac{2290}{4000}$$

$$= 0.5725$$

2) point estimate for population mean = sample mean

$$= \frac{5.4 + 1.1 + 0.42 + 0.73 + 0.48 + 1.1}{6}$$

$$= 1.54$$

3) standard error

4) $\hat{p} = 0.2$ $n = 3200$

$$se = \sqrt{\frac{\hat{p}(1-\hat{p})}{n}} = \sqrt{\frac{0.2(0.8)}{3200}} = 0.0071$$

5) $\hat{p} = \frac{23}{369} = 0.0623$ $n = 369$

$$se = \sqrt{\frac{\hat{p}(1-\hat{p})}{n}} = \sqrt{\frac{0.0623(1-0.0623)}{369}}$$

$$= 0.0126$$

$z = 1.96$ (for 95% confidence)

margin of error (me) = $z(se) = 1.96(0.0126) = 0.0247$.

confidence interval = $\hat{p} \pm me = 0.0623 \pm 0.0247$
 (95%)
 $= (0.0377, 0.0870)$

6) $\hat{p} = \frac{12}{346} = 0.0347$ $n = 346$

$se = \sqrt{\frac{\hat{p}(1-\hat{p})}{n}} = \sqrt{\frac{0.0347(1-0.0347)}{346}}$
 $= 0.00984$

$z = 2.33$ (for 98% confidence)

$me = z(se) = 2.33(0.00984) = 0.0229$

confidence interval = $\hat{p} \pm me = 0.0347 \pm 0.0229$
 (98%)
 $= (0.0118, 0.0576)$
 $= (0.012, 0.058)$

7) $me = z(se)$ for a proportion.

z depends on the confidence level (z increases as confidence level increases)

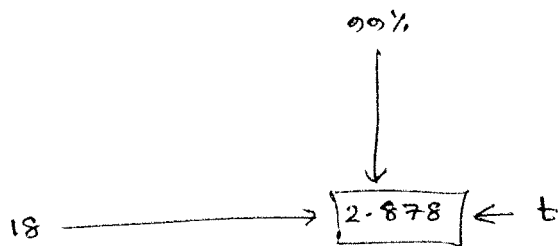
se depends on the sample size (se decreases as sample size increases)

$se = \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$

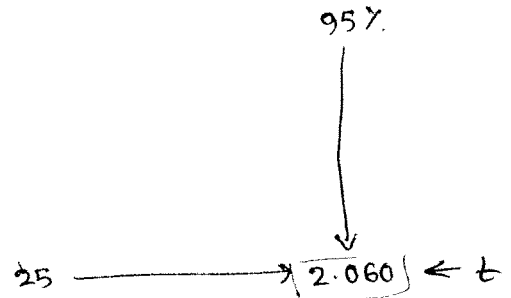
- therefore
- I X
 - II ✓
 - III ✓
 - IV X

∴ II and III will result in a larger me .

8) $df = 19 - 1 = 18$ ($df = n - 1$)



9) $df = 25$



10) confidence level $\downarrow \Rightarrow z \downarrow \Rightarrow me \downarrow$

③

(D)

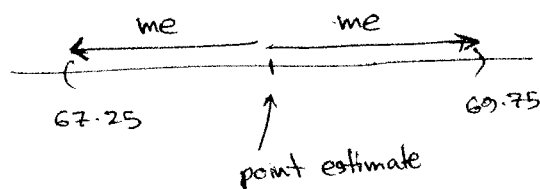
- 11)
- Population standard deviation is usually unknown. (This statement makes no difference)
 - For a population mean estimation, we need the assumption that the population is normally distributed. (This is also needed for both z and t intervals).
 - Sample size being small tells us that ~~we~~ we need to use a t interval. (If sample size is larger, t and z intervals will be equal in which case z interval could be used.)

Therefore (C).

[For a population proportion estimation, we always use z but we need $np \geq 15$ and $n(1-p) \geq 15$].

12) point estimate = sample mean = \$709

13) confidence interval = (67.25, 69.75)



$$\begin{aligned} \text{Therefore } me &= \frac{(69.75 - 67.25)}{2} \\ &= 1.25 \leftarrow (B) \end{aligned}$$

[If you were asked to find the point estimate, that would be $\frac{69.75 + 67.25}{2}$].

✖

14) point estimate = $\bar{x} = 68$ $n = 15$ $s = 2.3$

(Here what is given is the sample standard deviation. ~~So~~ we need to find the standard error)

$$se = \frac{s}{\sqrt{n}} = \frac{2.3}{\sqrt{15}} = 0.594$$

$df = n - 1 = 14$. Therefore ~~the value~~ $t = 1.761$ (for 90% confidence).

$$me = t \cdot (se) = 1.761 (0.594) = 1.046$$

$$\begin{aligned} \text{confidence interval} &= \bar{x} \pm me \\ &= 68 \pm 1.046 \\ &= (66.954, 69.046) \end{aligned}$$

15) point estimate = $\bar{x} = 1.3$ $n = 65$ $s = 1.1$

~~se = $\frac{s}{\sqrt{n}}$~~

$$se = \frac{s}{\sqrt{n}} = \frac{1.1}{\sqrt{65}} = 0.136$$

$$df = n - 1 = 64$$

Since we cannot find $df = 64$ in the table, using $df = 60$, we can get $t = 2$ for 95% confidence level

$$me = t(se) = 2(0.136) \\ = 0.272$$

$$\begin{aligned} \text{confidence interval} &= \bar{x} \pm me \\ &= 1.3 \pm 0.272 \\ &= (1.028, 1.572) \\ &= (1.03, 1.57) \end{aligned}$$