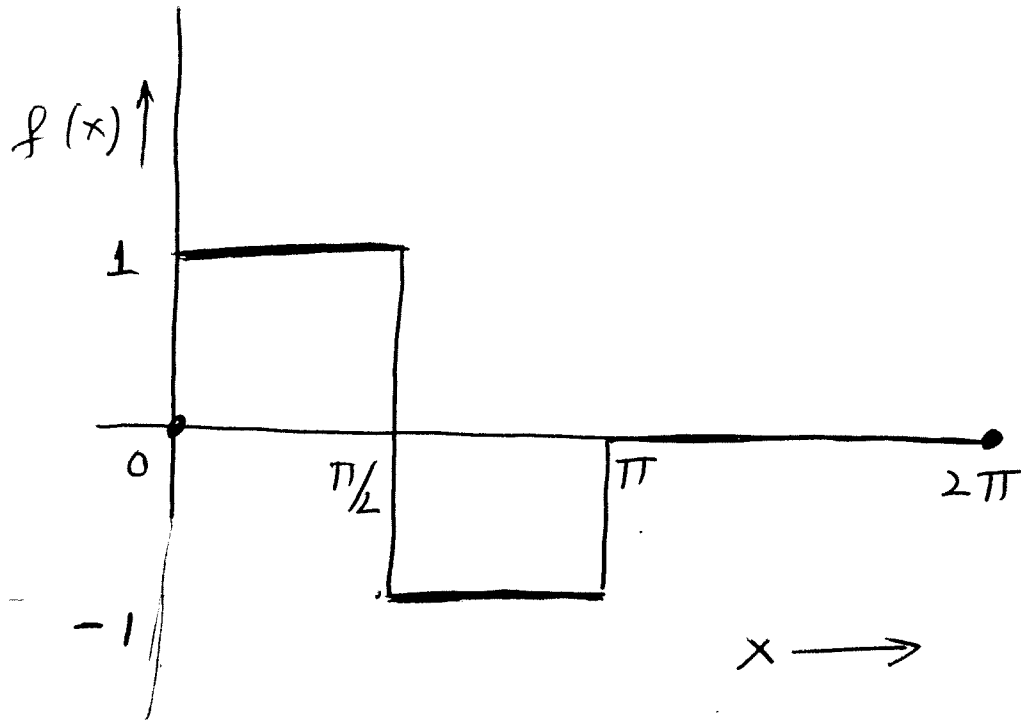


Third Test

Good Luck

Math 3350

①



We have a function  $f(x)$  defined in the interval  $[0, 2\pi]$  as shown above.

Assume that

$$f(x + 2\pi) = f(x) \text{ for all } x$$

ie  $f(x)$  has a period  $2\pi$ . Calculate the Fourier series expansion.

② consider the following differential equation

$$\frac{d^2 y}{dx^2} + 10 \frac{dy}{dx} + 21y = f(x).$$

choose

$$f(x) = \begin{cases} 1 & \text{for } x \geq 10 \\ 0 & \text{for } x < 10 \end{cases}$$

choose

$$y(0) = 0, \quad \frac{dy(0)}{dx} = 10$$

calculate  $y(x)$ .

③ calculate Laplace inverse of

$$\frac{3s+2}{s^2+4s+5}$$

④ For the differential equation

$$\frac{d^2 y}{dx^2} + \alpha \frac{dy}{dx} + \beta y = 0$$

we do not know  $\alpha, \beta$  but we know that for some initial condition  $y(0), \frac{dy(0)}{dx}$  the solution contains a term

$$y(x) = A e^{-5x} \cos 7x + \text{another term.}$$

(a) calculate  $\alpha$  and  $\beta$  if possible.

(b) calculate the other term in  $y(x)$  if possible